## **Supplemental information**



Fig. 5: HRXRD spectra of  $Ga_2O_3$  implanted with 4.8e15 cm<sup>-2</sup> Si<sup>+</sup> at (a) RT and at (b) HT, before and after annealing compared to the as-received MBE sample spectrum.